Alternating Current Chapter 24

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Alternating Quantities (*i* **or** *V***)**

(1) An alternating quantity (current *i* or voltage *V*) is one whose magnitude changes continuously with time between zero and a maximum value and whose direction reverses periodically.

(2) Some graphical representation for alternating quantities

(3) **Equation for** *i* **and** *V* **:** Alternating current or voltage varying as sine function can be written as

$$
i = i_0 \sin \omega t = i_0 \sin 2\pi v \, t = i_0 \sin \frac{2\pi}{7} \, t \tag{2}
$$
 Mean s
and
$$
V = V_0 \sin \omega t = V_0 \sin 2\pi v \, t = V_0 \sin \frac{2\pi}{7} \, t
$$

where *i* and *V* are Instantaneous *^V*⁰ or *ⁱ*⁰ Positive half 0 2 *T*/4 *i* or *V*

values of current and voltage,

 i_0 and V_0 are peak values of current and voltage

 ω = Angular frequency in *rad/sec*, $v =$ Frequency in *Hz* and *T* = time period

(i) The time taken to complete one cycle of variations is called the periodic time or time period.

(ii) Alternating quantity is positive for half the cycle and negative for the rest half. Hence average value of alternating quantity (*i* or *V*) over a complete cycle is zero.

(iii) The value of alternating quantity is zero or maximum 2ν times every second. The direction also changes 2ν times every second.

(iv) Generally sinusoidal waveform is used as alternating current/voltage.

(v) At $t = \frac{7}{4}$ from the beginning, *i* or *V* reaches to $t = \frac{T}{t}$ from the beginning, *i* or *V* reaches their maximum value.

Important Values of Alternating Quantities

(1) **Peak value** $(i_0$ or V_0) : The maximum value of alternating quantity (*i* or *V*) is defined as peak value or amplitude.

T (2) Modern square $\frac{2\pi}{\tau}$ *t* (2) Mean square value $(\overline{V^2} \text{ or } \overline{I^2})$: The average *T* called mean square value. It is always positive for π of square of instantaneous values in one cycle is

Fig. 24.2

T

T/2

–

Negative half cycle

t or

cycle **+**

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one complete cycle. *e.g.* $v^2 = \frac{1}{l} \int_0^l v^2 dt = \frac{v_0}{2}$ or $\int_{l_{\text{max}}} \frac{1}{l} dt = \frac{2i_0}{l} = 0.0$ $1 \int_{1}^{7} \int_{2}^{2} dt - \int_{0}^{2}$ or $\int_{1}^{7/2} t$ 0 2

$$
\overline{f^2} = \frac{\hat{f}_0^2}{2}
$$

(3) **Root mean square (r.m.s.) value :** Root of mean of square of voltage or current in an *ac* circuit for one complete cycle is called *r.m.s.* value. It is denoted by *Vrms* or *irms*

$$
i_{\text{rms}} = \sqrt{\frac{\hat{f}_1 + \hat{f}_2 + \dots}{n}} = \sqrt{\hat{f}^2} = \sqrt{\frac{\int_0^T \hat{f} dt}{\int_0^T dt}} = \frac{i_0}{\sqrt{2}} = 0.707 \quad i_0 = r.m.s. \text{ va}
$$

70.7% *i*⁰

Similarly
$$
V_{rms} = \frac{V_0}{\sqrt{2}} = 0.707 V_0 = 70.7\%
$$
 of V_0
\n
$$
\begin{bmatrix}\n\langle \sin^2(\omega t) \rangle = \langle \cos^2(\omega t) \rangle = \frac{1}{2}\n\end{bmatrix}
$$
\n $\begin{bmatrix}\n\sin^2(\omega t) = \langle \cos^2(\omega t) \rangle = \frac{1}{2}\n\end{bmatrix}$

(i) The *r.m.s.* value of alternating current is also called virtual value or effective value.

(ii) In general when values of voltage or current for alternating circuits are given, these are *r.m.s.* value.

(iii) ac ammeter and voltmeter are always measure *r.m.s.* value. Values printed on *ac* circuits are *r.m.s.* values.

(iv) In our houses *ac* is supplied at 220 *V*, which is the *r.m.s.* value of voltage. It's peak value is $\sqrt{2} \times 200 = 311V$.

(v) *r.m.s.* value of *ac* is equal to that value of *dc*, which when passed through a resistance for a given time will produce the same amount of heat as produced by the alternating current when passed through the same resistance for same time.

(4) **Mean or Average value** $(i_{av}$ or V_{av}) : The average value of alternating quantity for one complete cycle is zero.

The average value of ac over half cycle $(t = 0$ to *T*/2)

$$
\overline{V^2} = \frac{1}{T} \int_0^T V^2 dt = \frac{V_0^2}{2} \quad \text{or} \quad i_{av} = \frac{\int_0^{T/2} i dt}{\int_0^{T/2} dt} = \frac{2i_0}{\pi} = 0.637 i_0 = 63.7\% \quad \text{of } i_0,
$$

Similarly $V_{av} = \frac{2V_0}{\pi} = 0.637 V_0 = 63.7\% \text{ of } V_0.$

(5) **Peak to peak value :** It is equal to the sum of the magnitudes of positive and negative peak values

$$
\therefore
$$
 Peak to peak value = $V_0 + V_0 = 2V_0$

$$
= 2\sqrt{2} V_{rms} = 2.828 V_{rms}
$$

 $\frac{d^2y}{dx^2} = 0.707$ *i*₀ = (6) **Form factor and peak factor :** The ratio of *r.m.s.* value of *ac* to it's average during half cycle is defined as form factor. The ratio of peak value and *r.m.s.* value is called peak factor

Phase

Physical quantity which represents both the instantaneous value and direction of alternating quantity at any instant is called it's phase. It's a dimensionless quantity and it's unit is radian.

If an alternating quantity is expressed as $X = X_0 \sin(\omega t \pm \phi_0)$ then the argument of $\sin(\omega t + \phi)$ is called it's phase. Where $\omega t =$ instantaneous phase (changes with time) and ϕ_0 = initial phase (constant *w.r.t.* time)

Table 24.1 : Some important values

(1) **Phase difference** (Phase constant) : The difference between the phases of currents and voltage is called phase difference. If alternating voltage and current are given by $V = V_0 \sin(\omega t + \phi_1)$ and (1) improvement (z): $i = i_0 \sin(\omega t + \phi_2)$ then phase difference $\phi = \phi_1 - \phi_2$ (relative to current) or $\phi = \phi_2 - \phi_1$ (relative to voltage)

(2) **Time difference :** If phase difference between alternating current and voltage is ϕ then time difference between them is given as ϕ $T.D. = \frac{T}{2\pi} \times \phi$

 π

(3) **Phasor diagram :** A diagram representing alternating current and alternating voltage (of same frequency) as vectors (phasors) with the phase angle between them is called a phasor diagram.

While drawing phasor diagram for a pure element (*e.g. R*, *L* or *C*) either of the current or voltage can be plotted along *X*-axis.

But when phasor diagram for a combination of elements is drawn then quantity which remains constant for the combination must be plotted along *X*-axis so we observe that

(i) In series circuits current has to be plotted along *X*-axis.

(ii) In parallel circuits voltage has to be plotted along *X*-axis.

Measurement of Alternating Quantities

Alternating current shows heating effect only, hence meters used for measuring ac are based on heating effect and are called hot wire meters (Hot wire ammeter and hot wire voltmeter)

Impedance, Reactance, Admittance and Susceptance

(1) **Impedance (***Z***) :** The opposition offered by ac circuits to the flow of ac through it is defined it's impedance. It's unit is $ohm(\Omega)$.

(2) **Reactance** (X) : The opposition offered by inductor or capacitor or both to the flow of ac through it is defined as reactance. It is of following two type

(i) **Inductive reactance** (X_L) : Offered by inductive circuit $X_L = \omega L = 2\pi vL$ $v_{dc} = 0$ so for dc, $X_L =$ 0.

Capacitive reactance (X_C) : Offered by capacitive circuit $X_c = \frac{1}{\omega C} = \frac{1}{2\pi \nu C}$ for dc $X_c = \infty$.

(3) **Admittance** $(Y): Z = \frac{v_0}{\hbar} = \frac{v_{rms}}{\hbar}$ Reciprocal of *rms* V_{rms} **p** \cdot **1** \circ *i* $Z = \frac{V_0}{V} = \frac{V_{rms}}{V}$ Reciprocal of 0 $\frac{I_{rms}}{I_{rms}}$ σ μ ^{*rms*} Reciprocal of impedance is known as admittance $\left(Y=\frac{1}{Z}\right)$. It's unit $\left(Y=\frac{1}{Z}\right)$. It's unit is *mho*

(4) **Susceptance (***S***) :** the reciprocal of reactance is defined as susceptance $\left(S = \frac{1}{X}\right)$. It is of two type $\left(S = \frac{1}{X}\right)$. It is of two type

- (i) inductive susceptance $S_L = \frac{1}{X_L} = \frac{1}{2\pi vL}$ and $\sum_{L} = \frac{1}{X_L} = \frac{1}{2\pi v L}$ and
- (ii) Capacitive susceptance, $S_C = \frac{1}{X_C} = \omega C = 2\pi v C$. $B_C = \frac{1}{X_C} = \omega C = 2\pi v C$.

Power in ac Circuits

In dc circuits power is given by $P = Vi$. But in ac circuits, since there is some phase angle between voltage and current, therefore power is defined as the product of voltage and that component of the current which is in phase with the voltage.

Thus $P = V / \cos \phi$; where *V* and *i* are *r.m.s.* value of voltage and current.

(1) **Instantaneous power :** Suppose in a circuit *V* = V_0 sin ωt and $i = i_0 \sin(\omega t + \phi)$ then $P_{\text{instantaneous}} = V_i$ $= V_0 i_0 \sin \omega t \sin(\omega t + \phi)$

 $\theta \propto i$ of instantaneous power in an ac circuit over a full (2) **Average power (True power) :** The average cycle is called average power. It's unit is *watt i.e.*

$$
P_{av} = V_{rms}I_{rms} \cos \phi = \frac{V_0}{\sqrt{2}} \cdot \frac{i_0}{\sqrt{2}} \cos \phi = \frac{1}{2} V_0 i_0 \cos \phi = i_{rms}^2 R = \frac{V_{rms}^2 R}{Z^2}
$$

(3) **Apparent or virtual power :** The product of apparent voltage and apparent current in an electric circuit is called apparent power. This is always positive $P_{app} = V_{rms}i_{rms} = \frac{V_0 i_0}{2}$

Power Factor

(1) It may be defined as cosine of the angle of lag or lead $(i.e. cos \phi)$

(2) It is also defined as the ratio of resistance and impedance (*i.e.* $\frac{R}{Z}$) *R*

(3) The ratio $\frac{\text{True power}}{\text{Apparent power}} = \frac{W}{VA} = \frac{kW}{kVA} = \cos\phi$ (3) Phase difference between *VA kVA* (3) Phase diff

Resistive Circuit (*R***-Circuit)**

- (1) Current : $i = i_0 \sin \omega t$ R (2) Peak current : $i_0 = \frac{V_0}{R}$ \uparrow *i R i*
- (3) Phase difference between
- voltage and current : $\phi = 0^{\circ}$ (4) Power factor : $cos\phi = 1$ **Fig. 24.3**
- (5) Power : $P = V_{\text{rms}} i_{\text{rms}} = \frac{V_0 i_0}{2}$ $\pi/2$
- (6) Time difference : T.D. = 0
- (7) Phasor diagram : Both are in same phase

2 and 2

 \bar{V} **Fig. 24.4**

Inductive Circuit (*L***-Circuit)**

(7) Phasor diagram : Voltage leads the current by

or

Capacitive Circuit (*C***-Circuit)**

- *W* (1) Current : $i = i_0 \sin\left(\omega t + \frac{\pi}{2}\right)$ $\begin{array}{ccc} \n\end{array}$ $i = i_0 \sin \left(\omega t + \frac{\pi}{2}\right)$ C 2) \vert \vert π) and π (2) Peak current : $i_0 = \frac{v_0}{X_c} = V_0 \omega C = V_0 (2\pi\nu C)$ $i_0 = \frac{V_0}{X_C} = V_0 \omega C = V_0 (2\pi\nu C)$ *C i* $V = V_0 \sin \omega t$
	- *kVA* (3) Phase difference between voltage and current : $\phi = 90^\circ (or -\frac{\pi}{2})$ π . **Fig. 24.7**
- V_0 \downarrow \downarrow
- *R* (5) Power : $P = 0$
	- $V = V_0 \sin \omega t$ (6) Time difference : $TD = \frac{7}{4}$ 4 *T*
		- (7) Phasor diagram : Current leads the voltage by $\pi/2$

Fig. 24.8

Resistive, Inductive Circuit (*RL***-Circuit)**

(6) Power factor :
$$
\cos \phi = \frac{R}{\sqrt{R^2 + X_L^2}}
$$

(7) Leading quantity : Voltage

Resistive, Capacitive Circuit (*RC***-Circuit)**

- (1) Applied voltage : $V = \sqrt{V_R^2 + V_C^2}$ (2) Impedance : $Z = \sqrt{R^2 + X_C^2} = \sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}$ $\sum_{i=1}^{n}$ $Z = \sqrt{R^2 + X_C^2} = \sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}$
- (3) Current : $i = i_0 \sin(\omega t + \phi)$
- (4) Peak current : $i_0 = \frac{v_0}{Z} = \frac{v_0}{\sqrt{R_0^2 + x^2}} = \frac{v_0}{\sqrt{R_0^2 + x^2}}$ $\frac{V_0}{Z} = \frac{V_0}{\sqrt{R^2 + X_C^2}} = \frac{V_0}{\sqrt{R^2 + \frac{1}{2(1 - X_0^2)}}}$ (1) This can $\dot{b}_0 = \frac{V_0}{V_0} = \frac{V_0}{V_0} = \frac{V_0}{V_0}$ $+ X_C^2$ $\left|_{\mathcal{B}^2} \right|_{\mathcal{A}}$ 1 $=\frac{v_0}{c}=\frac{v_0}{c}=\frac{v_0}{c}=\frac{v_0}{c}$ $\overline{0}$ and $=$ $\frac{v_0}{\sqrt{2\pi}}$
- (5) Phase difference : $\phi = \tan^{-1} \frac{X_C}{S} = \tan^{-1} \frac{1}{S}$ (5) If net read
- (6) Power factor : $\cos \phi = \frac{R}{\sqrt{R^2 + X_C^2}}$ behaves as *LR* circ
(6) If net re

(7) Leading quantity : Current **Inductive, Capacitive Circuit (***LC***-Circuit)**

- (1) Applied voltage : $V = V_L V_C$ (ii) *V*
- (2) Impedance : $Z = X_i X_c = X$

(3) Current :
$$
i = i_0 \sin \left(\omega t \pm \frac{\pi}{2} \right)
$$
 (iii) F

(4) Peak current :
$$
i_0 = \frac{V_0}{Z} = \frac{V_0}{X_L - X_C} = \frac{V_0}{\omega L - \frac{1}{\omega C}}
$$
 (iv) Power

- (5) Phase difference : $\phi = 90^\circ$
- (6) Power factor : $\cos \phi = 0$ (vi)

(7) Leading quantity : Either voltage or current

Series *RLC***-Circuit**

- (1) **Equation of current** : $i = i_0 \sin(\omega t \pm \phi)$; where *Z V* $i_0 = \frac{v_0}{z}$
	- (2) **Equation of voltage :** From phasor diagram $V = \sqrt{V_R^2 + (V_L - V_C)^2}$
	- (3) **Impedance of the circuit :**

$$
\left(\frac{1}{C}\right)
$$
\n
$$
Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}
$$

V (4) **Phase difference :** From phasor diagram

$$
\frac{R^2 + \frac{1}{4\pi^2 v^2 C^2}}{\tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R} = \frac{\frac{\omega L - \frac{1}{\omega C}}{\omega C}}{R} = \frac{2\pi v L - \frac{1}{2\pi v C}}{R}
$$

 $\frac{dS}{dt} = \tan^{-1} \frac{1}{\omega CR}$ (5) If net reactance is inductive : Circuit behaves as *LR* circuit

 (6) **If net reactance is capacitive :** Circuit behave as *CR* circuit

> (7) **If net reactance is zero :** Means $X = X_1 - X_C = 0$

 $\Rightarrow X_L = X_C$. This is the condition of resonance

(8) **At resonance** (series resonant circuit)

(i) $X_L = X_C \implies Z_{\text{min}} = R$ *i.e.* circuit behaves as resistive circuit

(ii) $V_L = V_C \Rightarrow V = V_R$ *i.e.* whole applied voltage appeared across the resistance

- (iii) Phase difference : $\phi = 0^\circ \Rightarrow p.f. = \cos \phi = 1$
- V_0 *V*₀ $=$ V_0 *V*₀ $=$ V_{max} (iv) Power consumption $P = V_{\text{rms}} i_{\text{rms}} = \frac{1}{2} V_0 i_0$

 $\omega L - \frac{1}{\omega C}$ (v) Current in the circuit is maximum and it is *R V* $\dot{q}_0 = \frac{V_0}{\rho}$

> These circuit are used for voltage amplification and as selector circuits in wireless telegraphy.

(9) **Resonant frequency** (Natural frequency)

At resonance
$$
X_L = X_C
$$
 $\Rightarrow \omega_0 L = \frac{1}{\omega_0 C}$ $\Rightarrow \frac{2\pi}{T} \times \frac{\text{Max. energy stored}}{\text{Mean power dissipated}}$
\n $\omega_0 = \frac{1}{\sqrt{LC} \sec} \Rightarrow v_0 = \frac{1}{2\pi\sqrt{LC}} Hz$ (iv) $Q = \text{factor} - \frac{V_L}{V_C}$ or $\frac{V_C}{V_C}$

(Resonant frequency doesn't depend upon the resistance of the circuit)

(10) **Half power frequencies and band width :** The frequencies at which the power in the circuit is half of the maximum power (The power at resonance), are called half power frequencies.

(i) The current in the circuit at half power frequencies (HPF) is $\frac{1}{\sqrt{2}}$ or 0.707 or 70.7% of 2 and 2 1 or 0.707 or 70.70/ of maximum current (current at resonance). *Pmax* P_{\rightarrow} 2 $P = \frac{P_{\text{max}}}{P}$ ω_1 ω_0 ω_2 ν **Fig. 24.13**

(ii) There are two half power frequencies

(a) $\omega_1 \rightarrow$ called lower half power frequency. At this frequency the circuit is capacitive.

(b) $\omega_2 \rightarrow$ called upper half power frequency. It is greater than ω_0 . At this frequency the circuit is inductive.

(iii) Band width $(\Delta \omega)$: The difference of half power frequencies ω_1 and ω_2 is called band width $(\Delta \omega)$ and $\Delta \omega = \omega_2 - \omega_1$. For series resonant circuit it can be proved $\Delta \omega = \left(\frac{R}{L}\right)^2$ \int $\sqrt{2}$ (L) *R*

(11) **Quality factor (***Q***-factor) of series resonant circuit**

(i) The characteristic of a series resonant circuit is determined by the quality factor (*Q* - factor) of the circuit.

(ii) It defines sharpness of $i - v$ curve at resonance when *Q* - factor is large, the sharpness of resonance curve is more and vice-versa.

(iii) *Q* - factor also defined as follows

Parallel *RLC* **Circuits**

(1) **Current and phase difference :** From phasor diagram current $i = \sqrt{i_R^2 + (i_C - i_L)^2}$ and phase $\int_0^{2\pi}$ difference *G* $S_C - S_L$ l_R l_R *i* $i_C - i_L$ $_{t_{max}-1} (S_C - S_L)$ l_R *R* $\phi = \tan^{-1} \frac{(i_C - i_L)}{i} = \tan^{-1} \frac{(S_C - S_L)}{S}$ $\downarrow i_L$ i_R V *i iC iL iR* ϕ \tilde{v} **Fig. 24.16**

(2) **Admittance (***Y***) of the circuit :** From equation of current $\frac{V_0}{Z} = \sqrt{\left(\frac{V_0}{R}\right)^2 + \left(\frac{V_0}{X_L} - \frac{V_0}{X_C}\right)^2}$ \overline{a} \int $\int_0^2 + \left(\frac{V_0}{X_L} - \frac{V_0}{X_C}\right)^2$ $\left(\begin{array}{cc} V_0 & V_0 \end{array} \right)$ $\left(\overline{R}\right)^{-+}\left(\overline{X_{L}}-\overline{X_{C}}\right)$ $=\sqrt{\left(\frac{V_0}{R}\right)^2+\left(\frac{V_0}{X_L}-\frac{V_0}{X_C}\right)^2}$ *V*₀ *V*₀ 1 R \mid \mid X , X _c \mid V_0 ⁻ V_0 V_1 *Z* \parallel *R* \parallel *X X*_c \parallel *V*₀ | *V*₀ | *V*₀ *V*₀ | *V*₀ | *V*₀ | $\Rightarrow \frac{1}{Z} = Y = \sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2} = \sqrt{G^2 + (S_L - S_C)^2}$ \int_{0}^{2} $\sqrt{2(2-2)^{2}}$ $\left(\overline{X_L} - \overline{X_C}\right)$ = \sqrt{G} + $\left(\overline{S_L} - \overline{S_C}\right)$ $\int_{0}^{2} + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2 = \sqrt{G^2 + (S_L - S_C)^2}$ $\left(\frac{1}{R}\right)^2 + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2 = \sqrt{G^2 + (g^2)}$ $= Y = \sqrt{\left(\frac{1}{2}\right)^2 + \left(\frac{1}{2} - \frac{1}{2}\right)^2} = \sqrt{G^2 + (S_1 - S_2)}$ (3) **Resonance** : At resonance (i) $i_c = i_l \Rightarrow$

R $i_{\min} = i_R$

(ii)
$$
\frac{V}{X_C} = \frac{V}{X_L} \implies S_C = S_L \Rightarrow \Sigma S = 0
$$

(iii) $Z_{\text{max}} = \frac{V}{I_P} = R$ $Z_{\text{max}} = \frac{V}{i_R} = R$ (iv) $\phi = 0 \implies p.f. = \cos \phi = 1 = \text{maximum}$ (v) Resonant frequency $\Rightarrow v = \frac{1}{2\pi\sqrt{LC}}$ **Wattless Current** $1 \quad \cdots \quad \cdots \quad \cdots \quad \bullet$

(4) **Parallel** *LC* **circuits :** If inductor has resistance (*R*) and it is connected in parallel with capacitor as shown

(a)
$$
Z_{\text{max}} = \frac{1}{Y_{\text{min}}} = \frac{L}{CR}
$$
 cycle is

(b) Current through the circuit is minimum and $i_{min} = \frac{V_0 C R}{I}$

L (c) $S_L = S_C \Rightarrow \frac{1}{X_L} = \frac{1}{X_C} \Rightarrow X = \infty$ (d) Resonant frequency $\omega_0 = \sqrt{\frac{1}{LC} - \frac{H}{l^2}} \frac{I d\theta}{\theta c\theta}$ or

 $\frac{H}{L^2}$ *Hz*(Condition for parallel resonance is *R* LC l^2 \sim (commens for parameters commens in $\sigma_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$ Hz(Condition for parallel n $v_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{l^2}}$ Hz (Condition for parallel res $\frac{L}{C}$) $R<\sqrt{\frac{L}{C}}$

(e) Quality factor of the circuit $=\frac{1}{28}$. $\frac{1}{22}$. It is quadrate *LC* $=\frac{1}{CR}\cdot\frac{1}{\sqrt{1-R^2}}$. It is quadrature (90°) w

In the state of resonance the quality factor of the circuit is equivalent to the current amplification of the circuit.

(ii) If **inductance** has no resistance : If $R = 0$ then circuit becomes parallel *LC* circuit as shown

Condition of resonance : $i_c = i_l \Rightarrow \frac{V}{X_c} = \frac{V}{X_l}$ $V = V$

 $\Rightarrow X_c = X_l$. At resonance current *i* in the circuit is zero and impedance is infinite. Resonant

frequency : $v_0 = \frac{1}{2\pi\sqrt{LC}}$ Hz $I_0 = \frac{1}{2\sqrt{10}} Hz$

$\Rightarrow v = \frac{1}{2\sqrt{LC}}$ **Wattless Current**

In an ac circuit $R = 0 \Rightarrow \cos \phi = 0$ so $P_{av} = 0$ *i.e.* in resistance less circuit the power consumed is zero. Such a circuit is called the wattless circuit and the current flowing is called the wattless current.

or

The component of current which does not contribute to the average power dissipation is called wattless current

(i) The average of wattless component over one cycle is zero

(ii) Amplitude of wattless current = $i_0 \sin \phi$

 $\frac{1}{1}$ It is quadrature (90°) with voltage.

2 $\frac{1}{2} - \frac{R^2}{r^2}$ Choke Coil

L² Choke coil (or ballast) is a device having high inductance and negligible resistance. It is used to control current in ac circuits and is used in fluorescent tubes. The power loss in a circuit

(1) It consist of a *Cu* coil wound over a soft iron laminated core.

(2) Thick *Cu* wire is used to reduce the resistance (*R*) of the circuit.

(3) Soft iron is used to improve inductance (*L*) of the circuit.

(4) The inductive reactance or effective opposition of the choke coil is given by $X_L = \omega L =$ $2\pi vL$

(5) For an ideal choke coil $r = 0$, no electric energy is wasted *i.e.* average power $P = 0$.

(6) In actual practice choke coil is equivalent to a *R* – *L* circuit.

(7) Choke coil for different frequencies are made by using different substances in their core.

For low frequency *L* should be large thus iron core choke coil is used. For high frequency ac circuit, *L* should be small, so air cored choke coil is used.

 If ac is produced by a generator having a large number of poles then it's frequency

2 $v = \frac{\text{Number of poles} \times \text{rotation per second}}{2} = \frac{P \times n}{2}$ (a) Electric cu

Where P is the number of poles; n is the rotational frequency of the coil.

Alternating current in electric wires, bulbs etc. flows 50 times in one direction and 50 times in the opposite direction in 1 *second*. Since in one cycle the current becomes zero twice, hence a bulb lights up 100 times and is off 100 times in one second (50 cycles) but due to persistence of vision, it appears lighted continuously.

 \approx ac is more dangerous than dc.

 \approx The rate of change of ac is minimum at that instant when they are near their peak values.

as ac equipments such as electric motors, are

more durable and convenient compared to dc equipments.

Skin Effect

A direct current flows uniformly throughout the cross-section of the conductor. An alternating current, on the other hand, flows

mainly along the surface of the conductor. This effect is known as skin effect. the reason is that when alternating current flows through a conductor, the flux changes in the inner part of the conductor are higher. Therefore the inductance of the inner part is higher than that of the outer part. Higher the frequency of alternating current, more is the skin effect.

The depth upto which ac current flows through a wire is called skin depth (δ) .

- Ordinary Thinking

Objective Questions

Alternating Current, Voltage and Power

- **1.** The power is transmitted from a power house on high voltage ac because **[CPMT 1984, 85]**
- $=\frac{P\times n}{2}$ (a) Electric current travels faster at higher *volts*

(b) It is more economical due to less power wastage

(c) It is difficult to generate power at low voltage

(d) Chances of stealing transmission lines are minimized