



RK VISION ACADEMY

NEET | IIT – JEE | FOUNDATIONS

MATRIC PRACTICE PAPER (2024)

(Mathematics)

Grade: XII

Chapter: Applications Of Vector Algebra

Marks: 40 marks

Time: 90 minutes

SECTION A

(10x1=10)

Choose the correct option.

- Distance from the origin to the plane $3x-6y+2z+7=0$ is
 (a) 2 (b) 0 (c) 3 (d) 1
- If \vec{a} and \vec{b} are parallel vectors, then $[\vec{a}, \vec{c}, \vec{b}]$ is equal to
 (a) 1 (b) 2 (c) 0 (d) -1
- The angle between the lines $\frac{x-4}{2} = \frac{y}{1} = \frac{z+1}{-2}$ and $\frac{x-1}{4} = \frac{y+1}{-4} = \frac{z-2}{2}$ is
 (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{3}$ (c) $\frac{2\pi}{3}$ (d) $\frac{\pi}{4}$
- If the vectors $2\hat{i}-\hat{j}+3\hat{k}$; $3\hat{i}+2\hat{j}+\hat{k}$; $\hat{i}+m\hat{j}+4\hat{k}$ are coplanar, then the value of m is
 (a) 2 (b) 3 (c) -2 (d) -3
- The shortest distance between two given straight lines $\vec{r} = (2\hat{i}+3\hat{j}+4\hat{k}) + t(-2\hat{i}+\hat{j}-2\hat{k})$ and $\frac{x-3}{2} = \frac{y}{-1} = \frac{z+2}{2}$ is
 (a) $\frac{365}{3}$ (b) $\frac{\sqrt{365}}{3}$ (c) $\frac{365}{4}$ (d) $\frac{365}{\sqrt{3}}$
- If the line $\frac{x-2}{3} = \frac{y-1}{-5} = \frac{z+2}{2}$ lies in the plane $x+3y-\alpha z+\beta=0$, then (α, β) is
 (a) (-5,5) (b) (-6,7) (c) (5,-5) (d) (6,-7)
- If the direction cosines of a line are $\frac{1}{c}, \frac{1}{c}, \frac{1}{c}$, then
 (a) $c=\pm 3$ (b) $c=\pm\sqrt{3}$ (c) $c>0$ (d) $0<c<1$
- If the direction of the point (1,1,1) from the origin is half of its distance from the plane $x+y+z+k=0$, then the values of k are
 (a) ± 3 (b) ± 6 (c) -3,9 (d) 3,-9

9. If the length of the perpendicular from the origin to the plane $2x+3y+\lambda z=1$, $\lambda>0$ is $\frac{1}{5}$, then the value of λ is
 (a) $2\sqrt{3}$ (b) $3\sqrt{2}$ (c) 0 (d) 1
10. The angle between the line $\vec{r} = (\hat{i}+2\hat{j} - 3\hat{k}) + t(2\hat{i}+\hat{j} - 2\hat{k})$ and the plane $\vec{r} \cdot (\hat{i}+\hat{j}) + 4 = 0$ is
 (a) 0° (b) 30° (c) 45° (d) 90°

SECTION B

(3x2=6)

Answer the following.

11. Find the angle between the planes $\vec{r} \cdot (\hat{i}+\hat{j} - 2\hat{k}) = 3$ and $2x-2y+z=2$.
12. Show that the vectors $\hat{i}+2\hat{j} - 3\hat{k}$; $2\hat{i}-\hat{j} + 2\hat{k}$; $3\hat{i}+\hat{j} - \hat{k}$ are coplanar.
13. Verify whether the line $\frac{x-3}{-4} = \frac{y-4}{-7} = \frac{z+3}{12}$ lies in the plane $5x-y+z=8$.

SECTION C

(3x3=9)

Answer the following.

14. If $\vec{a}, \vec{b}, \vec{c}$ are three vectors, prove that $[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}] = 2[\vec{a}, \vec{b}, \vec{c}]$.
15. With usual notation, in any triangle ABC, prove by vector method that $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$.
16. Prove by vector method that the area of the quadrilateral ABCD having diagonal AC and BD is $\frac{1}{2}|\vec{AC} \times \vec{BD}|$.

SECTION D**(3x5=15)**

Answer the following.

17. Find the non-parametric form of vector and cartesian equation of the plane passing through the point (2,3,6) and parallel to the straight lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-3}{1}$ and $\frac{x+3}{2} = \frac{y-3}{-5} = \frac{z+1}{-3}$.
18. Find the vector equation and cartesian equation of a plane passing through the points (2,2,1), (9,3,6) and perpendicular to the plane $2x+6y+6z=9$.
19. Prove by vector method: $\sin(A+B) = \sin A \cos B + \cos A \sin B$.