



Assignment

Basic Limits

Basic Level

1. $\lim_{x \rightarrow \infty} \frac{(3x-1)(2x+5)}{(x-3)(3x+7)}$ is equal to

- (a) 3 (b) 2 (c) -2 (d) 1

2. $\lim_{x \rightarrow \infty} \frac{2x^2+3x+4}{3x^2+3x+4}$ is equal to

[SCRA 1996; Rajasthan PET 1987 ; BIT Ranchi 1998; MP PET 1993]

- (a) $\frac{2}{3}$ (b) 1 (c) 0 (d) ∞

3. $\lim_{x \rightarrow a} f(x).g(x)$ exists if

[Rajasthan PET 1995]

- (a) $\lim_{x \rightarrow a} f(x)$ and $\lim_{x \rightarrow a} g(x)$ exists (b) $\lim_{x \rightarrow a} f(x)^{g(x)}$ exists
(c) $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$ exists (d) $\lim_{x \rightarrow a} f(x)g\left(\frac{1}{x}\right)$ exists

4. $\lim_{x \rightarrow \infty} \left[x - \sqrt{x^2 + x} \right] =$

[IIT 1975]

- (a) $\frac{1}{2}$ (b) 1 (c) $-\frac{1}{2}$ (d) 0

5. If $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$ exists then

- (a) Both $\lim_{x \rightarrow a} f(x)$ and $\lim_{x \rightarrow a} g(x)$ must exist (b) $\lim_{x \rightarrow a} f(x)$ not exist but $\lim_{x \rightarrow a} g(x)$ exists
(c) Neither $\lim_{x \rightarrow a} f(x)$ nor $\lim_{x \rightarrow a} g(x)$ exists (d) $\lim_{x \rightarrow a} f(x)$ exist but $\lim_{x \rightarrow a} g(x)$ does not exist

6. Which of the following statement is not correct

(a) $\lim_{x \rightarrow c} [f(x) + g(x)] = \lim_{x \rightarrow c} f(x) + \lim_{x \rightarrow c} g(x)$

(b) $\lim_{x \rightarrow c} [f(x) - g(x)] = \lim_{x \rightarrow c} f(x) - \lim_{x \rightarrow c} g(x)$

(c) $\lim_{x \rightarrow c} [f(x).g(x)] = \lim_{x \rightarrow c} f(x) \cdot \lim_{x \rightarrow c} g(x)$

(d) $\lim_{x \rightarrow c} \frac{f(x)}{g(x)} = \frac{\lim_{x \rightarrow c} f(x)}{\lim_{x \rightarrow c} g(x)}$

7. $\lim_{x \rightarrow 3^-} \frac{|x-3|}{x-3} =$

- (a) 1 (b) -1 (c) 0 (d) Does not exist

8. $\lim_{x \rightarrow 3^+} \frac{|x-3|}{x-3} =$

- (a) 1 (b) -1 (c) 0 (d) Does not exist

9. If $\lim_{x \rightarrow a} \phi(x) = a^3, a \neq 0$ then $\lim_{x \rightarrow a} \phi\left(\frac{x}{a}\right)$ is equal to

- (a) a^2 (b) $\frac{1}{a^2}$ (c) $\frac{1}{a^3}$ (d) a^3

- 10.** If $\lim_{x \rightarrow a} \frac{a^x - x^a}{x^x - a^a} = -1$, then [EAMCET 2003]
 (a) $a = 1$ (b) $a = 0$ (c) $a = e$ (d) None of these
- 11.** $\lim_{x \rightarrow 4} \left[\frac{x^{3/2} - 8}{x - 4} \right] =$ [DCE 1999]
 (a) $\frac{3}{2}$ (b) 3 (c) $\frac{2}{3}$ (d) $\frac{1}{3}$
- 12.** $\lim_{x \rightarrow 0} \left[\frac{\sqrt{a+x} - \sqrt{a-x}}{x} \right] =$ [Karnataka CET 2001; Roorkee 1979; MP PET 1987]
 (a) 1 (b) 0 (c) \sqrt{a} (d) $\frac{1}{\sqrt{a}}$
- 13.** $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 + 5x + 8}}{4x + 5}$ is equal to
 (a) $-1/2$ (b) 0 (c) $1/2$ (d) 1
- 14.** $\lim_{x \rightarrow 4} \frac{3 - \sqrt{5+x}}{x-4}$ is equal to [Orissa JEE 1996]
 (a) $1/6$ (b) $-1/6$ (c) 0 (d) 1
- 15.** $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2 - 1}}{2x + 1}$ is equal to [BIT Ranchi 1992]
 (a) 1 (b) 0 (c) -1 (d) $\frac{1}{2}$
- 16.** $\lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x^2 + x - 6}$ equals [IIT 1970; IIT 1976])
 (a) $1/5$ (b) $2/5$ (c) 1 (d) 5
- 17.** The value of $\lim_{\theta \rightarrow 0} \left(\frac{\sin \theta / 4}{\theta} \right)$ is
 (a) 0 (b) $\frac{1}{4}$ (c) 1 (d) Note in existence
- 18.** $\lim_{x \rightarrow 0} \frac{x^2 - 2x}{2 \sin x}$ equals [Rajasthan PET 1985]
 (a) 1 (b) -1 (c) 0 (d) None of these
- 19.** $\lim_{x \rightarrow 0} \frac{\sin(2+x) - \sin(2-x)}{x} =$
 (a) $\sin 2$ (b) $2 \sin 2$ (c) $2 \cos 2$ (d) 2
- 20.** $\lim_{n \rightarrow \infty} (3^n + 4^n)^{\frac{1}{n}} =$ [Karnataka CET 2003]
 (a) 3 (b) 4 (c) ∞ (d) e
- 21.** True statement for $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{\sqrt{2+3x} - \sqrt{2-3x}}$ is [Ranchi BIT 1982; Haryana 1996])
 (a) Does not exist (b) Lies between 0 and $\frac{1}{2}$ (c) Lies between $\frac{1}{2}$ and 1
- 22.** $\lim_{x \rightarrow 1} \frac{(2x-3)(\sqrt{x}-1)}{2x^2+x-3} =$ [IIT 1977]
 (a) $-\frac{1}{10}$ (b) $\frac{1}{10}$ (c) $-\frac{1}{8}$ (d) None of these
- 23.** $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 8x + 3} - \sqrt{x^2 + 4x + 3}) =$ [MP PET 1997; Rajasthan PET 1995)]

90 Functions, Limits, Continuity and

(a) 0

(b) ∞

(c) 2

(d) $\frac{1}{2}$

24. $\lim_{x \rightarrow 0} \left(\frac{x^o}{\sin x^o} \right)$ equals

[AMU 1991]

(a) 1

(b) $\frac{\pi}{180}$

(c) $\frac{180}{\pi}$

(d) None of these

Advance Level

25. $\lim_{n \rightarrow \infty} \left[\frac{1^3 + 2^3 + 3^3 + \dots + n^3}{n^4} \right] =$

(a) $\frac{1}{2}$

(b) $\frac{1}{3}$

(c) $\frac{1}{4}$

(d) None of these

26. $\lim_{n \rightarrow \infty} \left[\frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} + \dots + \frac{1}{3n} \right] =$

[Karnataka CET 1999]

(a) 0

(b) $\log_e 4$

(c) $\log_e 3$

(d) $\log_e 2$

27. $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k}{n^2 + k^2} =$

[Roorkee 1999]

(a) $\left(\frac{1}{2}\right) \log 2$

(b) $\log 2$

(c) $\frac{\pi}{4}$

(d) $\frac{\pi}{2}$

28. The $\lim_{x \rightarrow 0} (\cos x)^{\cot x}$ is

[Rajasthan PET 1999]

(a) 0

(b) 1

(c) $\frac{1}{3}$

(d) $\frac{2}{3}$

29. $\lim_{x \rightarrow 0} \frac{x \tan 2x - 2x \tan x}{(1 - \cos 2x)^2} =$

[IIT 1999]

(a) 2

(b) -2

(c) $\frac{1}{2}$

(d) $-\frac{1}{2}$

30. If $f(x) = \sqrt{\frac{x - \sin x}{x + \cos^2 x}}$, then $\lim_{x \rightarrow \infty} f(x)$ is

[DCE 2000; EAMCET 1997]

(a) 0

(b) ∞

(c) 1

(d) Not exist

31. If $f(x) = \begin{cases} x & ; \quad x < 0 \\ 1 & ; \quad x = 0, \\ x^2 & ; \quad x > 0 \end{cases}$, then, $\lim_{x \rightarrow 0} f(x) =$

[DCE 2000]

(a) 0

(b) 1

(c) 2

(d) Does not exist

32. If $f(x) = \begin{cases} \sin x & , \quad x \neq n\pi \\ 0 & , \text{ other wise} \end{cases}, \quad n \in \mathbb{Z}$ $g(x) = \begin{cases} x^2 + 1 & , \quad x \neq 0, 2 \\ 4 & , \quad x = 0 \\ 5 & , \quad x = 2 \end{cases}$, then $\lim_{x \rightarrow 0} g\{f(x)\} =$

[Karnataka CET 2000]

(a) 1

(b) 0

(c) $\frac{1}{2}$

(d) $\frac{1}{4}$

33. $\lim_{n \rightarrow \infty} \frac{1^p + 2^p + 3^p + \dots + n^p}{n^{p+1}} =$

[AIEEE 2002]

(a) $\frac{1}{p+1}$

(b) $\frac{1}{1-p}$

(c) $\frac{1}{p} - \frac{1}{(p-1)}$

(d) $\frac{1}{p+2}$

- 34.** $\lim_{n \rightarrow \infty} \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \dots + \frac{1}{2^n}$ equals [Rajasthan PET 1996]
 (a) 2 (b) -1 (c) 1 (d) 3
- 35.** $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{\sin^{-1} x} =$
 (a) 2 (b) 1 (c) -1 (d) None of these
- 36.** $\lim_{x \rightarrow 0} \cos \frac{1}{x}$ [UPSEAT 2002]
 (a) Is continuous at $x=0$ (b) Differentiable at $x=0$ (c) Does not exist (d) None of these
- 37.** If $x_n = \frac{1-2+3-4+5-6+\dots-2n}{\sqrt{n^2+1}+\sqrt{4n^2-1}}$, then $\lim_{n \rightarrow \infty} x_n$ is equal to
 (a) $\frac{1}{3}$ (b) $-\frac{1}{3}$ (c) $\frac{2}{3}$ (d) 1
- 38.** $\lim_{n \rightarrow \infty} \left[\frac{1}{n} + \frac{1}{\sqrt{n^2+n}} + \frac{1}{\sqrt{n^2+2n}} + \dots + \frac{1}{\sqrt{n^2+(n-1)n}} \right]$ is equal to [Rajasthan PET 2000]
 (a) $2+2\sqrt{2}$ (b) $2\sqrt{2}-2$ (c) $2\sqrt{2}$ (d) 2
- 39.** $\lim_{n \rightarrow \infty} \frac{1}{1^3+n^3} + \frac{4}{2^3+n^3} + \dots + \frac{1}{2n}$ is equal to [Rajasthan PET 1995]
 (a) $\frac{1}{3} \log_e 3$ (b) $\frac{1}{3} \log_e 2$ (c) $\frac{1}{3} \log_e \frac{1}{3}$ (d) None of these
- 40.** The value of $\lim_{n \rightarrow \infty} \left[\frac{n}{1+n^2} + \frac{n}{4+n^2} + \frac{n}{9+n^2} + \dots + \frac{1}{2n} \right]$ is equal to
 (a) e (b) $\frac{1}{e}$ (c) $\frac{\pi}{4}$ (d) $\frac{4}{\pi}$
- 41.** $\lim_{x \rightarrow \infty} \frac{x^n}{e^x} = 0$ for
 (a) No value of n (b) n is any whole number (c) $n=0$ only (d) $n=2$ only

Exponential and Logarithmic Limits
Basic Level

- 42.** $\lim_{x \rightarrow 0} \left[\tan \left(\frac{\pi}{4} + x \right) \right]^{1/x}$ is equal to [Rajasthan PET 2001]
 (a) e^{-1} (b) e (c) e^2 (d) \sqrt{e}
- 43.** $\lim_{x \rightarrow 0} \left(\frac{3^x - 1}{x} \right)$ equals [Rajasthan PET 1998]
 (a) $\log 3$ (b) $3 \log 3$ (c) $2 \log 3$ (d) None of these
- 44.** $\lim_{x \rightarrow 0} \frac{\cos(\sin x) - 1}{x^2} =$ [Orissa JEE 2003]
 (a) 1 (b) -1 (c) 1/2 (d) -1/2
- 45.** $\lim_{x \rightarrow 0} \frac{e^{1/x}}{\frac{1}{e^x} + 1} =$ [DCE 1999]
 (a) 0 (b) 1 (c) Does not exist (d) None of these

92 Functions, Limits, Continuity and

46. $\lim_{x \rightarrow 0} \frac{a^{\sin x} - 1}{b^{\sin x} - 1} =$

[Karnataka CET 2000]

- (a) $\frac{a}{b}$ (b) $\frac{b}{a}$

(c) $\frac{\log a}{\log b}$

(d) $\frac{\log b}{\log a}$

47. $\lim_{x \rightarrow 0} \left(\frac{e^x - 1}{x} \right) =$

[Karnataka CET 2001]

(a) $\frac{1}{2}$

(b) ∞

(c) 1

(d) 0

48. $\lim_{x \rightarrow \infty} \left(\frac{x+3}{x+1} \right)^{x+1} =$

[Rajasthan PET 2003]

- (a) e^2 (b) e^3

(c) e

(d) e^{-1}

49. $\lim_{x \rightarrow 0} (1 - ax)^{\frac{1}{x}} =$

[Karnataka CET 2003]

- (a) e (b) e^{-a}

(c) 1

(d) e^a

Advance Level

50. $\lim_{x \rightarrow \infty} \left(\frac{x-3}{x+2} \right)^x$ is equal to

[IIT 2000]

- (a) e (b) e^{-1} (c) e^{-5} (d) e^5

51. $\lim_{x \rightarrow 0} \left(\frac{1+5x^2}{1+3x^2} \right)^{1/x^2}$ is

[IIT 1996]

- (a) e^2 (b) e (c) e^{-1} (d) None of these

52. The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2 - 2x + 1}{x^2 - 4x + 2} \right)^x$ is equal to

- (a) e^2 (b) e^{-2} (c) e^6 (d) None of these

53. $\lim_{x \rightarrow \infty} \left[1 + \frac{1}{mx} \right]^x$ equal to

[Haryana CEE 1998]

- (a) $e^{1/m}$ (b) $e^{-1/m}$ (c) e^m (d) m^e

54. $\lim_{x \rightarrow \infty} \left(\frac{x^2 + 5x + 3}{x^2 + x + 3} \right)^x =$

[AIEEE 2002]

- (a) e^4 (b) e^2 (c) e^3 (d) e

55. $\lim_{x \rightarrow 0} \frac{x \cdot 2^x - x}{1 - \cos x}$ is equal to

[IIT 1980; BIT Ranchi 1983; Rajasthan PET 1999, 2001]

- (a) $\log 2$ (b) $\log 4$ (c) 0 (d) None of these

56. $\lim_{x \rightarrow 0} \left(\frac{a^x - b^x}{x} \right) =$

[EAMCET 1988; Rajasthan PET 1995]

(a) $\log\left(\frac{b}{a}\right)$

(b) $\log\left(\frac{a}{b}\right)$

(c) $\frac{a}{b}$

(d) $\log a^b$

57. $\lim_{x \rightarrow \infty} \frac{\log x^n - [x]}{[x]}, n \in N, ([x] \text{ denotes greatest integer less than or equal to } x)$ [AIEEE 2002]
 (a) Has value -1 (b) Has value 0 (c) Has value 1 (d) Does not exist

Trigonometric Limits
Basic Level

58. $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2 x)}{x^2} =$ [MP PET 2002; UPSEAT 2001; IIT Screening 2001]

(a) $-\pi$

(b) π

(c) $\frac{\pi}{2}$

(d) 1

59. $\lim_{x \rightarrow 0} \left\{ \frac{\sin x - x + \frac{x^3}{6}}{x^5} \right\} =$ [MNR 1985; MNR 1986)]

(a) $\frac{1}{120}$

(b) $-\frac{1}{120}$

(c) $\frac{1}{20}$

(d) None of these

60. $\lim_{x \rightarrow 0} \frac{\sqrt{\frac{1}{2}(1 - \cos 2x)}}{x} =$ [Rajasthan PET 2001; AIEEE 2002]
 (a) 1 (b) -1 (c) 0 (d) Does not exist

61. $\lim_{x \rightarrow \pi/4} \frac{\sqrt{2} \cos x - 1}{\cot x - 1} =$ [BIT Ranchi 1989; IIT 1990]

(a) $\frac{1}{\sqrt{2}}$

(b) $\frac{1}{2}$

(c) $\frac{1}{2\sqrt{2}}$

(d) 1

62. $\lim_{x \rightarrow a} \frac{\cos x - \cos a}{\cot x - \cot a} =$ [BIT Ranchi 1987]
 (a) $\frac{1}{2} \sin^3 a$

(b) $\frac{1}{2} \operatorname{cosec}^2 a$

(c) $\sin^3 a$

(d) $\operatorname{cosec}^3 a$

Advance Level

63. $\lim_{x \rightarrow \infty} \sqrt{\frac{x + \sin x}{x - \cos x}} =$ [Roorkee 1994]

(a) 0

(b) 1

(c) -1

(d) None of these

64. The value of $\lim_{n \rightarrow \infty} \cos\left(\frac{x}{2}\right) \cos\left(\frac{x}{4}\right) \cos\left(\frac{x}{8}\right) \dots \cos\left(\frac{x}{2^n}\right)$ is

(a) 1

(b) $\frac{\sin x}{x}$

(c) $\frac{x}{\sin x}$

(d) None of these

65. If x is a real number in $[0,1]$, then the value of $\lim_{m \rightarrow \infty} \lim_{n \rightarrow \infty} [1 + \cos^{2m}(n! \pi x)]$ is given by

(a) 2 or 1 according as x is rational or irrational
 (c) 1 for all x

(b) 1 or 2 according as x is rational or irrational
 (d) 2 or 1 for all x

94 Functions, Limits, Continuity and

66. $\lim_{x \rightarrow 0} \frac{1 - \cos 5x}{2^x - 3^x}$ is equal to
 (a) 0 (b) 1 (c) 5 (d) None of these
67. If $\lim_{x \rightarrow 0} \frac{x^n - \sin x^n}{x - \sin^n x}$ is non zero definite, then n must be
 (a) 1 (b) 2 (c) 3 (d) None of these
68. The values of a and b such that $\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$, are
 (a) $\frac{5}{2}, \frac{3}{2}$ (b) $\frac{5}{2}, -\frac{3}{2}$ (c) $-\frac{5}{2}, -\frac{3}{2}$ (d) None of these
69. $\lim_{h \rightarrow 0} \frac{2 \left[\sqrt{3} \sin \left(\frac{\pi}{6} + h \right) - \cos \left(\frac{\pi}{6} + h \right) \right]}{\sqrt{3}h(\sqrt{3} \cos h - \sin h)} =$ [BIT Ranchi 1987]
 (a) $-\frac{2}{3}$ (b) $-\frac{3}{4}$ (c) $-2\sqrt{3}$ (d) $\frac{4}{3}$
70. If $f(x) = \int \frac{2 \sin x - \sin 2x}{x^3} dx$, then $\lim_{x \rightarrow 0} f'(x)$ equals [IIT Screening 1997]
 (a) 0 (b) 1 (c) -1 (d) 1/2

L'- Hospital Rule

Basic Level

71. $\lim_{x \rightarrow 0} \frac{x}{\tan^{-1}(2x)}$ is equal to [IIT 1992; Rajasthan PET 2001]
 (a) 0 (b) 1 (c) $\frac{1}{2}$ (d) None of these
72. $\lim_{x \rightarrow 0} \frac{e^{\tan x} - e^x}{\tan x - x}$ is equal to [Rajasthan PET 2001]
 (a) 0 (b) 1 (c) e (d) $\frac{1}{e}$
73. $\lim_{x \rightarrow \pi/2} (\sec x - \tan x)$ equals [Rajasthan PET 1998]
 (a) 0 (b) 1 (c) -1 (d) None of these
74. $\lim_{x \rightarrow 0} \frac{2 \sin^2 3x}{x^2} =$ [Roorkee 1982; DCE 1999]
 (a) 0 (b) 1 (c) 18 (d) 36
75. $\lim_{x \rightarrow 0} \frac{\sin 2x}{x} =$ [MNR 1990; UPSEAT 2000]
 (a) 0 (b) 1 (c) 1/2 (d) 2
76. If $f(1) = 1$ and $f'(1) = 4$, then the value of $\lim_{x \rightarrow 1} \frac{\sqrt{f(x)} - 1}{\sqrt{x} - 1}$ is [DCE 2001]
 (a) 9 (b) 4 (c) 12 (d) 1
77. $\lim_{x \rightarrow 0} \frac{\log_e(1+x)}{3^x - 1} =$ [MP PET 2002]
 (a) $\log_e 3$ (b) 0 (c) 1 (d) $\log_3 e$
78. $\lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{\sin x} =$ [Haryana CEE 2002]
 (a) 0 (b) 1 (c) 2 (d) Non existent

79. $\lim_{x \rightarrow -2} \frac{\sin^{-1}(x+2)}{x^2 + 2x} =$ [Orissa JEE 2002]
 (a) 0 (b) ∞ (c) $-\frac{1}{2}$ (d) None of these
80. $\lim_{x \rightarrow a} \frac{(x^{-1} - a^{-1})}{x - a} =$ [MP PET 1994]
 (a) $\frac{1}{a}$ (b) $-\frac{1}{a}$ (c) $\frac{1}{a^2}$ (d) $-\frac{1}{a^2}$
81. $\lim_{x \rightarrow 1} \frac{\log x}{x-1}$ is equal to [Rajasthan PET 1996; MP PET 1996]
 (a) 1 (b) 0 (c) -1 (d) 1/2
82. $\lim_{x \rightarrow 1} \frac{1-x^{-1/3}}{1-x^{-2/3}} =$
 (a) $\frac{1}{3}$ (b) $\frac{1}{2}$ (c) $\frac{2}{3}$ (d) $-\frac{2}{3}$

Advance Level

83. The value of $\lim_{x \rightarrow 0} \frac{x \cos x - \log(1+x)}{x^2}$ is [Rajasthan PET 1999]
 (a) $\frac{1}{2}$ (b) 0 (c) 1 (d) None of these
84. $\lim_{x \rightarrow \frac{\pi}{4}} \left(\frac{1 - \tan x}{1 - \sqrt{2} \sin x} \right)$ equals [SCRA 1999]
 (a) 0 (b) 1 (c) -2 (d) 2
85. $\lim_{x \rightarrow 0} \frac{2^x - 1}{\sqrt{1+x} - 1}$ equals [Karnataka CET 1999, IIT 1983]
 (a) $\log 2$ (b) $\log 4$ (c) $\log 3$ (d) None of these
86. $\lim_{x \rightarrow 0} \left[\frac{\sin(x+a) + \sin(a-x) - 2 \sin a}{x \sin x} \right]$ is equal to [UPSEAT 1998]
 (a) $\sin a$ (b) $-\sin a$ (c) 1 (d) 0
87. $\lim_{x \rightarrow \pi/2} \frac{\int_{\pi/2}^x t dt}{\sin(2x - \pi)}$ is equal to [MP PET 1998]
 (a) ∞ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{8}$
88. $\lim_{y \rightarrow 0} \frac{(x+y)\sec(x+y) - x \sec x}{y} =$
 (a) $\sec x(x \tan x + 1)$ (b) $x \tan x + \sec x$ (c) $x \sec x + \tan x$ (d) None of these
89. $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin\left(\frac{\pi}{3} - x\right)}{2 \cos x - 1}$ is equal to [AMU 1991]
 (a) $\frac{1}{2}$ (b) $\frac{1}{\sqrt{3}}$ (c) $\sqrt{3}$ (d) $\frac{2}{\sqrt{3}}$
90. $\lim_{x \rightarrow 0} \frac{e^{x^2} - \cos x}{x^2}$ is equal to [AMU 1990]
 (a) $\frac{1}{2}$ (b) $\frac{1}{\sqrt{3}}$ (c) $\sqrt{3}$ (d) $\frac{2}{\sqrt{3}}$

96 Functions, Limits, Continuity and

(a) $\frac{3}{2}$

(b) $\frac{1}{2}$

(c) $\frac{2}{3}$

(d) None of these

91. $\lim_{x \rightarrow 0} \frac{x \cos x - \sin x}{x^2 \sin x}$ equals

[SCRA 1999]

(a) $\frac{1}{3}$

(b) $-\frac{1}{3}$

(c) 3

(d) -3

Answer Sheet

Assignment (Basic & Advance Level)